# The Genetics of $\mathrm{LD}_{2}$. I. Gene Frequency: An Estimation 

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THE existence of $\mathrm{LD}_{2}$ has been inferred from crossing-over families in which weak MLC stimulation occurs between the recombinant ( R ) and his HLA-D identical siblings (S). ${ }^{1-9}$

This locus, which controls weakly stimulatory determinants, appears to be located in the proximity of HLA-A, as indicated by the finding that some HLA-A/C or A/B recombinants respond to and/or stimulate slightly lymphocytes from siblings that differ only for the HLA-A region. ${ }^{1-9}$ We have suggested that the $\mathrm{LD}_{2}$ locus is of restricted polymorphism, since $\mathrm{LD}_{2}$ differences were absent in a large proportion of previously reported HLA-A/B and in all HLA-B/D crossing-over families. ${ }^{8}$

Our present report on 16 recombinant families informative for $\mathrm{LD}_{2}$ ( $8 \mathrm{HLA}-\mathrm{A} / \mathrm{B}$ and $8 \mathrm{HLA}-\mathrm{B} / \mathrm{D}$ ) and on the results of MLCs between unrelated HLA-D-identical individuals is consistent with the above hypothesis.

## MATERIALS AND METHODS

All reported families were completely typed, on at least two different occasions, for HLA-A, B, C, D, DR, and Bf and tested in intrafamilial mixed lymphocyte cultures (MLCs) using previously described procedures. ${ }^{10-13}$ The following criteria were used for ascertaining $\mathrm{LD}_{2}$ differences between R and S : (1) following the triple normalization procedure, the response in one or in both directions had to be at least threefold higher than the autocontrol values, yet consistently lower than that induced by one-haplotype (HLA-D) difference; (2) when $R$ had more than one HLA-D-identical sibling, all of the latter ones had to display the same pattern of response to R ; (3) HLA-D identity between $R$ and $S$ had to be confirmed by HTC-typing, DR typing, or, in the case of unidentified HLA-D alleles, by PLT typing with reagents prepared within the family against each parental haplotype. ${ }^{11}$

Ten blood group systems and 15 biochemical markers were determined by standard techniques and legitimacy of offspring was confirmed in all recombinant families. ${ }^{14}$

Unrelated HLA-D-identical individuals were selected from an HLA-A, B, C, D, DR genotyped panel of 100 families. The strength of MLC responses in checkerboard experiments was quantitated by cluster analysis. ${ }^{12}$

Responses in cluster 0 are considered negative, cluster 1 weak positive, clusters 2 and 3 positive.

RESULTS
Estimation of $L D_{2}$ Gene Frequency in Recombinant Families

Sixteen crossing-over families (8 HLA$\mathrm{A} / \mathrm{B}$ and $8 \mathrm{HLA}-\mathrm{B} / \mathrm{D})$ in which the recombinant had at least one HLA-D-identical sibling are included in this analysis. The MLC stimulation patterns between the recombinant and one of his HLA-D-identical siblings were: (A) reciprocal nonstimulation; (B) one-way stimulation; (C) two-way stimulation. The following distribution was observed:

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Pattern A
    HLA-A/B : }3\mathrm{ HLA-B/D : 5
Pattern B
    HLA-A/B:2 HLA-B/D : 2
Pattern C
    HLA-A/B : 3 HLA-B/D : 1
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Since the HLA-D-identical, $\mathrm{LD}_{2}$-different children share one nonrecombinant haplotype, carrying, for example, the allele a, the other parent in which the recombination occurred should be: (1) aa or bb for pattern $A$; (2) $a b$ for pattern $B$; and (3) bc for pattern C. Thus a minimum of three $\mathrm{LD}_{2}$ alleles should be considered.

For $n \mathrm{LD}_{2}$ alleles, pattern A is expected in $n(n+1) / 2 ; \mathrm{B}$ in $n(n-1)$; and C in $n(n-1)(n-2) / 2 \mathrm{LD}_{2}$-informative sib

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Table 1. Estimation of $L D_{2}$ Gene Frequency: Recombinant Families

| Pattern of MLC | Type of R-S Combination | Number of Possible Combinations for $n L_{2}$ Alleles | Frequency of Patterns for $n$ Alleles |
| :---: | :---: | :---: | :---: |
| (A) No stimulation | aa-aa | $n$ | $P_{1} \times P_{1}^{2}$ |
|  | $a b-a b$ | $\binom{n}{2}=\frac{n(n-1)}{2}$ | $P_{1} \times P_{1}^{2}$ |
| Total |  | $n+\frac{n(n-1)}{2}=\frac{n(n+1)}{2}$ | $\sum_{i=1} P_{i}\left(P_{i}^{2}+\sum_{i=1} P_{i}^{2}\right)=\sum_{i=1} P_{i} \sum_{i=1} P_{i}^{2}=\sum_{i=1} P_{i}^{2}$ |
| (B) One-way |  |  | ${ }_{1=1}^{1+1} \sum_{i=1}^{1=1}$ |
| stimulation | $a \mathrm{a}-\mathrm{ab}$ | $n(n-1)$ | $P_{1} \times{ }_{n}{ }_{2} P_{j} P_{k}$ |
| Total |  |  | $2 \sum P_{i}^{2}\left(\sum P_{i}\right)=2 \sum P_{i}^{2}\left(1-P_{i}\right)$ |
| (C) Two-way |  |  |  |
| stimulation | ab-ac |  | $P_{i} \times 2 P_{i} P_{k}$ |
| Total |  | $n\binom{n-1}{2}=\frac{n(n-1)(n-2)}{2}$ | $2 \sum^{n} P_{i}\left(\sum_{j<k} P_{i} P_{k}\right)=\sum^{n} P_{i}\left(1-\sum^{n} P_{i}^{2}-2 P_{i} \sum P_{i}\right)$ |

pairs (Table 1). Assuming $n \mathrm{LD}_{2}$ alleles $\left(A_{1}, \ldots, A_{n}\right)$ with frequencies $P_{1}, \ldots, P_{n}$ and $\sum_{i=1}^{n} P_{i}=1$, the three patterns will fit into the following equations:
(A) $\sum_{i=1}^{n} P_{i}^{2}$
(B) $2 \cdot \sum_{i=1}^{n} P_{i}^{2}\left(1-p_{i}\right)$
(C) $1-\sum_{i=1}^{n} P_{i}^{2}-2 \cdot \sum_{i=1}^{n} P_{i}^{2}\left(1-P_{i}\right)$

The distribution of the stimulation patterns in
our crossing-over series cannot fit these equations unless one $\mathrm{LD}_{2}$ allele has an $r f>0.5$

## Estimation of $L D_{2}$ Gene Frequency in

 Unrelated HLA-D-Identical IndividualsIt is possible that $\mathrm{LD}_{2}$ also contributes to MLC stimulation between pairs of HLA-D-identical unrelated individuals. In this case, reciprocal stimulation (pattern C) would include not only $\mathrm{LD}_{2}$ half-identical

Table 2. Estimation of $L_{\mathbf{2}}$ Gene Frequency: Nonrecombinant Families

| Pattern of MLC | Type of MLC Combination | Number of Possible Combinations for $n \mathrm{LD}_{2}$ Alleles | Frequency of Patterns for $n$ Alleles |
| :---: | :---: | :---: | :---: |
| (A) No stimulation |  |  |  |
| Type 1 | aa-aa | $n$ | $P_{i}^{2} \times P_{i}^{2}=P_{i}^{\text {d }}$ |
| Type 2 | $a b-a b$ | $\left(_{2}^{n}\right)=\frac{n(n-1)}{2}$ | $2 P_{i} P_{i} \times 2 P_{i} P_{i}=4 P_{i}^{2} P_{j}^{2}$ |
| Total |  | $n+\frac{n(n-1)}{2}=\frac{n(n+1)}{2}$ | $\sum^{n} P_{i}^{1}+4 \sum P_{i}^{2} P_{i}^{2}$ |
| (B) One-way stimulation i=1 ki |  |  |  |
| Type | $a \mathrm{a}-\mathrm{ab}$ | $n(n-1)$ | $P_{i}^{2} \times{ }_{n} 2 P_{i} P_{j}=2 P_{i}^{3} P_{j}$ |
| Total |  |  | $2 \sum\left(P_{i}^{3} \sum P_{i}\right)=2 \sum P_{i}^{3}\left(1-P_{i}\right)$ |
|  |  |  |  |
| Type 1 | aa-bb | $\left(_{2}^{n}\right)=\frac{n(n-1)}{2}$ | $P_{I}^{2} \times P_{I}^{2}$ |
| Type 2 | $\mathrm{ab}-\mathrm{ac}$ | $n\binom{n-1}{2}=\frac{n(n-1)(n-2)}{2}$ | $2 P_{i} P_{j} \times 2 P_{i} P_{k}=4 P_{i}^{2} P_{j} P_{k}$ |
| Type 3 | $a \mathrm{a}-\mathrm{bc}$ | $n\binom{n-1}{2}=\frac{n(n-1)(n-2)}{2}$ | $P_{l}^{2} \times 2 P_{j} P_{k}$ |
| Type 4 | ab-cd | $3\left({ }_{4}^{n}\right)=\frac{n(n-1)(n-2)(n-3)}{8}$ | $2{ }_{2} P_{l} P_{j} \times 2 P_{k} P_{1}=4 P_{i} P_{j} P_{k} P_{1}$ |
| Total |  | $\frac{n(n-1)\left(n^{2}+3 n-6\right)}{8}$ | $1-\sum_{i=1}^{n} P_{i}^{i}-4 \sum_{i<1} P_{i}^{2} P_{i}^{2}-2 \sum_{i=1}^{n} P_{i}^{3}\left(1-P_{i}\right)$ |

pairs ( ab with ac ), as in crossing-over families, but also individuals differing by both $\mathrm{LD}_{2}$ alleles.

Table 2 shows the type of $\mathrm{LD}_{2}$ combinations expected to result in the three patterns of MLC stimulations, the number of possible combinations for $n \mathrm{LD}_{2}$ alleles, and the frequency of the different patterns.

This model has been tested in two different ways. The first one consisted of determining the frequency of the 3 patterns of MLC stimulation in 90 pairs of unrelated individuals heterozygous for the same HLA-D alleles (Table 3). No stimulation occurred in $44 \%$, one-way stimulation in $33 \%$, and two-way stimulation in $23 \%$ of MLCs within HLA-D-identical pairs.

The second approach consisted of testing 14 unrelated individuals, homozygous for Dw3 (Dw3-HTCs) in a single checkerboard MLC.

Each of these HTCs was previously documented to be Dw3-DRw3 homozygous by complete family segregation studies. In addition, they were all tested as stimulators on a selected panel comprising 40 Dw3-heterozygous individuals.

Four Dw3-heterozygous individuals were
included as responders and stimulators in the checkerboard experiment. Table 4 illustrates the results obtained by triple normalization and cluster analysis of MLC responses between the 14 Dw3 homozygotes. Reciprocal nonstimulation was observed in 44/182 (24\%) reactions, one-way stimulation or responsiveness in 72/182 (39\%), and reciprocal stimulation in 66/182 (36\%) reactions. Three groups of reciprocally nonstimulatory Dw3 HTCs were found. The first comprises 6 individuals (nos. 1-6); the second, 4 individuals (nos. 7-10); the third, only 2 (nos. 11 and 12). Two HTCs (nos. 13 and 14) were reciprocally stimulatory in MLC with all the other Dw3 homozygotes. The first group reacted against, yet failed to stimulate, all HTCs from the second and third groups. This observation, in conjunction with the level of stimulation seen in MLCs between cells from different groups, is consistent with the possibility that the $\mathrm{LD}_{2}$ type is $x x$ for individuals $1-6, x y$ for $7-10, x z$ for 11 and $12, y z$ for no. 13 , and $z w$ for no. 14. The frequency of the $x$, $y, z$, and, $w \mathrm{LD}_{2}$ alleles would then be $.64, .18$, .14 , and .036 , respectively, with no significant differences between the observed and expected number of $\mathrm{LD}_{2}$-homozygous and

Table 3. MLC Responses Within Pairs of HLA-D-Identical Unrelated Individuals

|  | No. of Individuals | No. of Pairs | Patterns of MLC Stimulation |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | (A) None | (B) <br> One-way | (C) <br> Two-way |
| Dw1, Dw2 | 3 | 6 | 4 | 0 | 2 |
| Dw1, Dw3 | 4 | 12 | 12 | 0 | 0 |
| Dw1, Dw4 | 2 | 2 | 2 | 0 | 0 |
| Dw1, Dw7 | 4 | 12 | 2 | 2 | 8 |
| Dw2, Dw3 | 4 | 12 | 12 | 0 | 0 |
| Dw2, Dw4 | 3 | 6 | 0 | 2 | 4 |
| Dw2, Dw5 | 3 | 6 | 2 | 4 | 0 |
| Dw3, Dw4 | 2 | 2 | 2 | 0 | 0 |
| Dw3, Dw5 | 4 | 12 | 0 | 8 | 4 |
| Dw4, Dw5 | 4 | 12 | 0 | 8 | 4 |
| Dw4, Dw6 | 2 | 2 | 2 | 0 | 0 |
| Dw4, Dw7 | 3 | 6 | 2 | 2 | 2 |
| Dw5, Dw7 | 3 | 6 | 2 | 4 | 0 |
| Dw5, Dw 11 | 3 | 6 | 2 | 4 | 0 |
| Dw 10, Dw 11 | 2 | 2 | 2 | 0 | 0 |
| Total | 46 | 104 | 46 (44\%) | 34 (33\%) | 24 (23\%) |

Table 4. Clusters of MLC Responses in a Checkerboard Between Dw3 HTCs

| HLA (-A,B) Haplotypes | Responders | Stimulators |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| 1,8/28,8 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 |
| 1,8/28,8 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 |
| 1,8/1,8 | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 |
| 1,8/1,8 | 4 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 |
| 1,8/1,8 | 5 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 |
| 1,8/2,35 | 6 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 |
| 11,8/23,50 | 7 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| 1,8/1,8 | 8 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| 1,8/1,8 | 9 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| 1,8/1,8 | 10 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| 1,8/2,8 | 11 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |
| 1,8/24,8 | 12 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |
| 1,8/1,8 | 13 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 |
| 1,8/30,8 | 14 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 1 | 1 | 1 | 0 |

-heterozygous individuals:

|  | $x x$ | $x y$ | $x z$ | $x w$ |
| :--- | :---: | :---: | :---: | :---: |
| Expected | 5.74 | 3.22 | 2.50 | .64 |
| Observed | 6.00 | 4.00 | 2.00 | 0 |
|  | $y y$ | $y z$ | $y w$ |  |
| Expected | .45 | .71 | .18 |  |
| Observed | 0 | 1.00 | 0 |  |
|  | $z z$ | $z w$ | $w w$ |  |
| Expected | .27 | .14 | .018 |  |
| Observed | 0 | 1.00 | 0 |  |

These results fit with the equations presented in Table 2. They are also in general agreement with the frequency of cluster-0 stimulation induced in the Dw3-heterozygous panel by the Dw3 HTC from the first group ( $\simeq 90 \%$ ), second group ( $\simeq 40 \%$ ), HTC 13
( $\sim 25 \%$ ), and $14(<5 \%)$. Nevertheless, it is equally possible that stimulation between unrelated HLA-D-identical individuals reflects the complexity of the HLA-D region, in which distinct, but closely linked, (sub)loci or multiple alleles at a single locus might code for antigenic determinants constituting the same HLA-D cluster.

## CONCLUSION

Data obtained from HLA-A/B and B/D recombinant families, which were informative for $\mathrm{LD}_{2}$, as well as from MLCs between HLA-D-identical unrelated individuals, suggest that $\mathrm{LD}_{2}$ is a locus of a restricted polymorphism, possibly having 4 alleles of which one has a frequency $>.50$.

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